

# Calculation of Some Geometric Elements of Conical Wheels with Circularly Arched Teeth

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## Abstract

*This paper shows the method for calculating the main geometric elements of the conical gear with circularly arched teeth type 528 Saratov.*

**Key words:** *wheel, gear, module, division diameter, the head diameter*

## General Considerations

Wheels with slanted teeth are used in conditions of peripheral velocities less than 12 m/s, and wheels with round teeth are recommended and used for velocities between 3 and 40 m/s (fig. 1) [1, 2].

For greater velocities, the teeth are rectified after the thermal improvement treatment, in which case wheels with circularly arched teeth are used.

Conic gears with round teeth function silently, have a great degree of coverage, high durability to usage, and allow the making of high engagement ratios compared to other types of conic gears, have a small gauge and reduced axial forces.

These types of concurrent conic gears are usually orthogonal.

The slanting direction of the teeth (left-right or reverse, as seen from the tip of the wheel's cone (fig. 1) is established according to the rotation direction of the leading wheel, such that the effect of the axial force (axial component) is to increase the matching of the teeth, avoiding any blockages [3, 4].

The slanting angles of the teeth are: the exterior dividing slanting angle,  $\beta_e$ , the interior dividing slanting angle,  $\beta_i$ , the angle between a radial perpendicular line that intersects the dividing line of a flank of the cog of the plane wheel of defining reference, in a point found at the exterior, interior extremity of the teeth and the tangent at that point to the dividing line of the flank of the teeth of the plane wheel (fig. 2).

The principle that lies at the base of the processing of conic wheel with circularly arched teeth consists of generating a single cog of the plane wheel through an imaginary plane wheel materialized through the teething tool (fig. 3) [5].

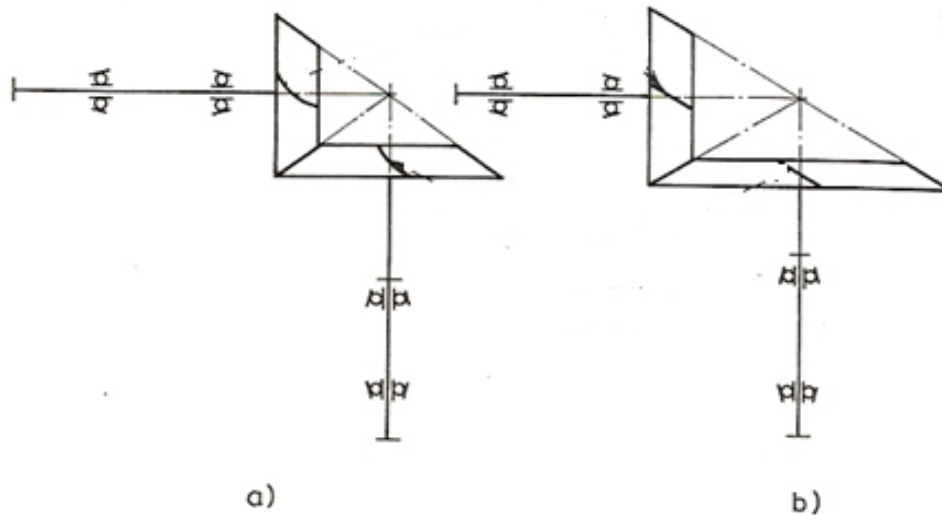


Fig 1. Conic gears with: a - round teeth; b- slanted teeth

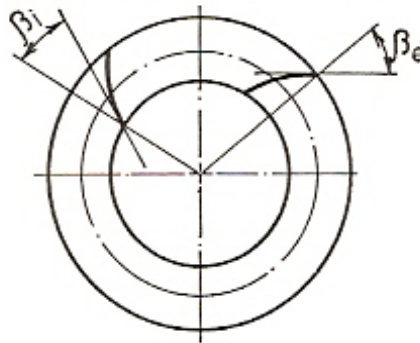


Fig.2. The exterior dividing slanting angle  $\beta_e$  and the interior dividing slanting angle  $\beta_i$

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The main geometric elements of the conic gear with circularly arched teeth are shown in Figure 4 and are determined as such:

- the exterior (frontal) module:  $m$ ;
- the coefficient for the width of the teeth:

$$k_b = \frac{R}{b} = (3 \dots 4), \quad (1)$$

where  $R$  is the (exterior) length of the division generator, and  $b$  is the width of the teeth;

- the coefficient for the radial movement of the pinion profile:  
- of the pinion (1):

$$x_{r1} = 0,49 \cdot \cos \left[ \beta \left( 1 - \frac{1}{u^2} \right) \right], \quad (2)$$

where  $\beta$  is the median slanting angle, and  $u$  is the engagement ratio;

- at the wheel (2):

$$x_{r2} = -x_{r1} ; \tag{3}$$

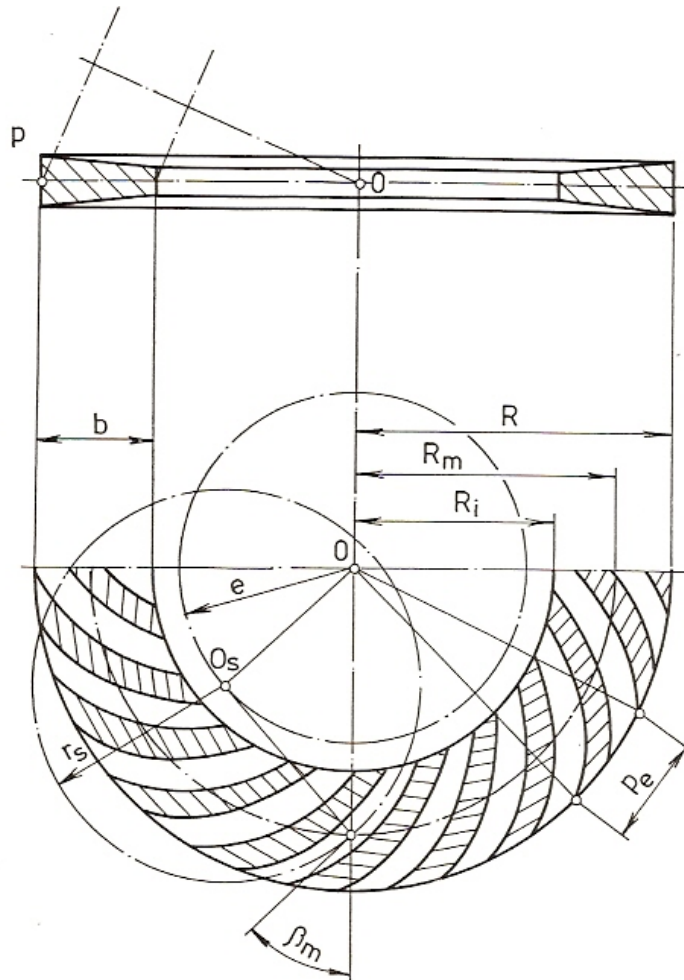


Fig. 3. Plane wheel of the circularly arched teeth

- angle of the dividing cone:  
- of the pinion (1):

$$\delta_1 = \arctg \left( \frac{1}{u} \right); \tag{4}$$

- of the wheel (2):

$$\delta_2 = \arctg u ; \tag{5}$$

- (interior) module:

$$m_t = m \cdot \frac{k_b - 1}{k_b} ; \tag{6}$$

- exterior division slating angle:

$$\sin \beta_e = \frac{2 \cdot k_b - 1}{2 \cdot k_b} \cdot \sin \beta + \left[ 1 - \left( \frac{2 \cdot k_b - 1}{2 \cdot k_b} \right)^2 \right] \cdot \frac{R}{D_s} \tag{7}$$

where  $D_s$  is the nominal diameter of the tool head [6];

- interior division slating angle:

$$\sin \beta_i = \frac{2 \cdot k_b - 1}{2 \cdot (k_b - 1)} \cdot \sin \beta + \frac{3 - 4 \cdot k_b}{4 \cdot (k_b - 1)} \cdot \frac{R}{D_s \cdot k_b} \quad (8)$$

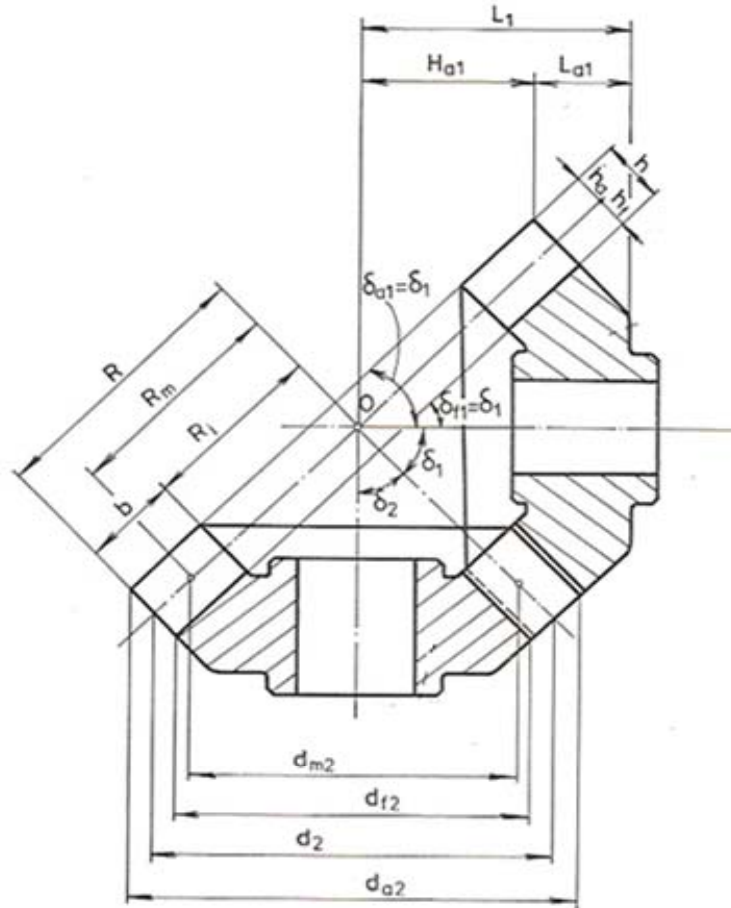


Fig 4. Geometric elements of conic gears with circularly arched cogs of constant height

### Calculation of Control Elements for Circularly Arched Teeth and Constant Height 528 Saratov Model

- cog frontal division arc:
  - at the pinion (1):

$$s_{t1} = \frac{\pi m}{2} + 2 \cdot \frac{x_{r1} \cdot \operatorname{tg} \alpha_n}{\cos \beta_s} \quad (9)$$

where  $\alpha_n$  is the normal division pressure angle ( $\alpha_n = 20^\circ$ );

- at the wheel (2):

$$s_{t2} = \pi \cdot m - s_{t1} \quad (10)$$

- intermediate coefficient:

$$G_s = \frac{1}{2} \cdot \sin \beta_s \cdot \cos \beta_s \quad (11)$$

- reduction coefficient of the cog:
  - at the pinion (1) :

$$k_1 = 1 - \frac{s_{t1}}{R} \cdot G_2; \quad (12)$$

$$k_2 = 1 - \frac{s_{t2}}{R} \cdot G_2; \quad (13)$$

- central half-angle corresponding to the girth of the cog in the normal section:
  - at the pinion (1) :

$$\omega_1 = \frac{s_{t1}}{d_1} \cdot \cos^2 \beta_g \cdot \cos \theta_1; \quad (14)$$

- at the wheel (2):

$$\omega_2 = \frac{s_{t2}}{d_2} \cdot \cos^2 \beta_g \cdot \cos \theta_2; \quad (15)$$

where  $d_1$  is the division diameter of the pinion ( $d_1 = m z_1$ ), and  $d_2$  is the division diameter of the wheel ( $d_2 = m z_2$ );

- coefficients calculation:
  - at the pinion (1) :

$$k_{11} \cong 1 - \frac{\omega_1^2}{6}; k_{21} \cong \frac{\omega_1}{4}; \quad (16)$$

- at the wheel (2):

$$k_{12} \cong 1 - \frac{\omega_2^2}{6}; k_{22} \cong \frac{\omega_2}{4}; \quad (17)$$

- cog width measured on a constant chord at the exterior extremity:
  - at the pinion (1):

$$s_{c1} = k_{11} \cdot s_{t1} \cdot k_1 \cdot \cos \beta_g; \quad (18)$$

- at the wheel (2):

$$s_{c2} = k_{12} \cdot s_{t2} \cdot k_2 \cdot \cos \beta_g; \quad (19)$$

- sharpness of the cog:
  - at the pinion (1):

$$\Delta h_1 = k_{21} \cdot s_{c1} \cdot \cos \beta_g; \quad (20)$$

- at the wheel (2):

$$\Delta h_2 = k_{22} \cdot s_{c2} \cdot \cos \beta_g; \quad (21)$$

- height measured at the constant chord:
  - at the pinion (1):

$$h_{c1} = h_{a1} + k_1 \cdot \Delta h_1; \quad (22)$$

- at the wheel (2):

$$h_{c2} = h_{a2} + k_2 \cdot \Delta h_2; \quad (23)$$

$h_{a1}$  and  $h_{a2}$  represent the height of the (division) head of the cog for the pinion and the wheel having the mathematical expressions:

$$h_{a1} = (h_a^* + x_{r1}) \cdot m_f; \quad (24)$$

$$h_{a2} = (h_a^* + x_{r2}) \cdot m_f; \quad (25)$$

where  $h_a^*$  is the coefficient of the reference hard of the cog ( $h_a^* = 1.0$ ).

## Conclusions

Considering the special advantages of these types of gears (high coverage degree, etc.) this paper shows the method for calculating the main geometric elements of conic wheel with circularly arched cogs of constant height 528 Saratov.

The rigorous calculations of the control elements for the circularly arched cogs of constant height must also be noted.

## References

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## Calculul unor elemente geometrice ale roților conice cu dantura în arc de cerc

### Rezumat

*Angrenajele conice cu dantura în arc de cerc au o largă utilizare în construcția de mașini datorită unor avantaje deosebite ca : funcționare silențioasă, grad mare de acoperire, etc. În lucrare se prezintă modul de calcul al principalelor elemente geometrice ale roților conice cu dinți în arc de cerc de înălțime constantă 528 Saratov. Lucrarea are o aplicabilitate practică imediată atât în ce privește proiectarea angrenajelor conice cu dantură în arc de cerc cât și privitor la repararea utilajelor tehnologice care au în componența lor angrenaje conice.*